

Thermalization of pair plasma with proton loading

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Pair plasma in GRBs

Why e^+e^- pairs?

- Energy range: $10^{48} < E_0 < 10^{54}$ erg

(isotropic energy release, fraction of stellar mass)

- Size range: $10^6 < R_0 < 10^8$ cm

(time variability, NS-BH size)

Optical depth for pair production: $\tau = \sigma_T n_\gamma R \approx \sigma_T E_0 / R_0^2 \gg 1$.

Why baryons?

- Time duration of the whole burst, spectrum
- Progenitors of GRBs: massive stars, NS

Issues:

- ① Microphysics: processes, baryonic loading, ...
- ② Macrophysics: global dynamics, geometry, ...
- ③ Radiation: mechanisms, transparency, ...

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- Intensity of interactions between photons and other particles $\tau = n \sigma R$.
- **Plasma degeneracy** $\theta_F = \left[\left(\frac{\hbar}{mc} \right)^2 (3\pi^2 n_-)^{\frac{2}{3}} + 1 \right]^{1/2} - 1$.

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- In our energy range $\epsilon \lesssim 10$ MeV the plasma is non-degenerate $\theta_F > \theta_{th}$.
- **Natural parameters for perturbative expansion are α and m/M .**

Proton loading

When admixture of **protons** and electrons is allowed it is characterized by a new parameter, the baryonic loading

$$\mathbf{B} = \frac{NMc^2}{\mathcal{E}_\gamma} = \frac{n_p Mc^2}{\rho_\gamma}. \quad (1)$$

In equilibrium, while e^+e^- are relativistic, $\epsilon_\pm \sim mc^2 \sim k_B T$, protons are not $Mv_p^2 \sim k_B T$, and thus

$$\frac{v_p}{c} \sim \sqrt{\frac{m}{M}}.$$

Also in equilibrium with $\epsilon_\pm \geq mc^2$ we have $\rho_\pm \approx n_\pm mc^2$ and thus

$$\frac{n_p}{n_\pm} \sim \frac{m}{M} B.$$

If in addition **neutrons** are present, they are coupled to protons by elastic nuclear scattering.

Pair plasma is transparent to **neutrinos**.

Interactions with pairs

Binary interactions	Radiative and pair producing variants
Møller and Bhabha scattering $e_1^\pm e_2^\pm \longrightarrow e_1^{\pm'} e_2^{\pm'}$ $e^\pm e^\mp \longrightarrow e^{\pm'} e^{\mp'}$	Bremsstrahlung $e_1^\pm e_2^\pm \longleftrightarrow e_1^{\pm'} e_2^{\pm'} \gamma$ $e^\pm e^\mp \longleftrightarrow e^{\pm'} e^{\mp'} \gamma$
Single Compton scattering $e^\pm \gamma \longrightarrow e^\pm \gamma'$	Double Compton scattering $e^\pm \gamma \longleftrightarrow e^{\pm'} \gamma' \gamma''$
Pair production and annihilation $\gamma \gamma' \longleftrightarrow e^\pm e^\mp$	Radiative pair production and three photon annihilation $\gamma \gamma' \longleftrightarrow e^\pm e^\mp \gamma''$ $e^\pm e^\mp \longleftrightarrow \gamma \gamma' \gamma''$
	$e^\pm \gamma \longleftrightarrow e^{\pm'} e^{\mp'} e^{\pm''}$

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	$p e_1^\pm \longleftrightarrow p' e_1^{\pm'} e^\pm e^\mp$
Single Compton scattering $p \gamma \longrightarrow p' \gamma'$	Double Compton scattering and radiative pair production $p \gamma \longleftrightarrow p' \gamma' \gamma''$
	$p \gamma \longleftrightarrow p' e^\pm e^\mp$

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- **Proton Compton scattering:**

$$(n_p t_{\gamma p})^{-1} \approx \left(\frac{\epsilon}{Mc^2}\right)^2 (n_- t_{\gamma e})^{-1}, \quad \epsilon \geq mc^2.$$

Boltzmann equation

Relativistic Boltzmann equations in spherically symmetric case

$$\frac{1}{c} \frac{\partial f_i}{\partial t} + \beta_i \left(\mu \frac{\partial f_i}{\partial r} + \frac{1 - \mu^2}{r} \frac{\partial f_i}{\partial \mu} \right) - \nabla U \frac{\partial f_i}{\partial \mathbf{p}} = \sum_q (\eta_i^q - \chi_i^q f_i), \quad (2)$$

where $\mu = \cos \vartheta = \mathbf{r} \cdot \mathbf{p}$, U is a potential due to some external force, $\beta_i = v_i / c$, $f_i(\epsilon, t)$ are distribution functions, and η_i^q and χ_i^q are the emission and the absorption coefficients. This is a coupled system of partial-integro-differential equations.

For homogeneous and isotropic distribution functions of electrons, positrons and photons (2) reduces to

$$\frac{1}{c} \frac{\partial f_i}{\partial t} = \sum_q (\eta_i^q - \chi_i^q f_i). \quad (3)$$

In (3) we also explicitly neglect the Vlasov term.

Collisional integrals 1: probability

Differential probability for all processes per unit time and unit volume ($\hbar = c = 1$)

$$dw = (2\pi)^4 \delta^{(4)}(P_f - P_i) \frac{|M_{fi}|^2}{\prod_b 2\epsilon_b} \prod_a \frac{d\mathbf{p}'_a}{(2\pi\hbar)^3},$$

where $\mathbf{p}'_a$ are momenta of outgoing particles, ϵ_b are energies of particles before and after interaction, M_{fi} are corresponding matrix elements, $\delta^{(4)}$ stands for energy-momentum conservation.

As example consider absorption coefficient for Compton scattering

$$\chi^{\gamma e^\pm \rightarrow \gamma' e^\pm} f_\gamma = \int d\mathbf{k}' d\mathbf{p} d\mathbf{p}' w_{\mathbf{k}', \mathbf{p}'; \mathbf{k}, \mathbf{p}} f_\gamma(\mathbf{k}, t) f_\pm(\mathbf{p}, t),$$

where $\mathbf{p}$ and $\mathbf{k}$ are momenta of electron (positron) and photon respectively, $d\mathbf{p} = d\epsilon_\pm d\phi_\pm \beta_\pm / c^3$, $d\mathbf{k}' = d\epsilon'_\gamma d\phi'_\gamma / c^3$.

Collisional integrals 2: integration over momentum

We can perform one integration over $d\mathbf{p}'$ as

$\int d\mathbf{p}' \delta(d\mathbf{k} + d\mathbf{p} - d\mathbf{k}' - d\mathbf{p}') \rightarrow 1$, but it is necessary to take into account the momentum conservation in the next integration over $d\mathbf{k}'$,

$$\begin{aligned} & \int d\epsilon'_\gamma \delta(\epsilon_\gamma + \epsilon_\pm - \epsilon'_\gamma - \epsilon'_\pm) = \\ &= \int d(\epsilon'_\gamma + \epsilon'_\pm) \frac{1}{|\partial(\epsilon'_\gamma + \epsilon'_\pm)/\partial\epsilon'_\gamma|} \delta(\epsilon_\gamma + \epsilon_\pm - \epsilon'_\gamma - \epsilon'_\pm) \rightarrow \\ & \rightarrow \frac{1}{|\partial(\epsilon'_\gamma + \epsilon'_\pm)/\partial\epsilon'_\gamma|} \equiv J_{\text{cs}}, \end{aligned}$$

where the Jacobian of the transformation is

$$J_{\text{cs}} = \frac{1}{1 - \beta'_\pm \mathbf{b}'_\gamma \cdot \mathbf{b}'_\pm}, \quad (4)$$

where $\mathbf{b}_i = \mathbf{p}_i/p$, $\mathbf{b}'_i = \mathbf{p}'_i/p'$, $\mathbf{b}'_\pm = (\beta_\pm \epsilon_\pm \mathbf{b}_\pm + \epsilon_\gamma \mathbf{b}_\gamma - \epsilon'_\gamma \mathbf{b}'_\gamma)/(\beta'_\pm \epsilon'_\pm)$.

Collisional integrals 3: three-particle interactions

Finally, for the absorption coefficient

$$\chi^{\gamma e^{\pm} \rightarrow \gamma' e^{\pm'}} f_{\gamma} = - \int d\omega'_{\gamma} d\mathbf{p} \frac{c\epsilon'_{\gamma} |M_{fi}|^2}{16\epsilon_{\pm}\epsilon_{\gamma}\epsilon'_{\pm} c^3 (2\pi\hbar)^2} J_{cs} f_{\gamma}(\mathbf{k}, t) f_{\pm}(\mathbf{p}, t),$$

As example of 3-particle reaction consider relativistic bremsstrahlung $e_1 + e_2 \leftrightarrow e'_1 + e'_2 + \gamma'$. For the time derivative, for instance, of the distribution function f_2 one has

$$\begin{aligned} \dot{f}_2 = & \int dp'_2 dk' (2\pi)^4 \delta^{(4)}(P_f - P_i) \frac{|M_{fi}|^2}{2^5 \epsilon_1 \epsilon_2 \epsilon'_1 \epsilon'_2 \epsilon'_{\gamma}} \times \\ & \times \left(\int \frac{d\mathbf{p}'_1 f'_k d\mathbf{p}_1 f'_1 f'_2}{(2\pi\hbar)^6} - \int \frac{d\mathbf{p}_1 d\mathbf{p}'_1 f_1 f_2}{(2\pi\hbar)^9} \right). \end{aligned}$$

In the case of kinetic equilibrium we have multipliers proportional to $\exp \frac{\varphi}{k_B T}$ in front of the integrals. The calculation is then reduced to the known thermal equilibrium case.

Detailed balance conditions (pure pair plasma)

Consider distribution functions

$$f_{\gamma} = \frac{1}{\exp\left(\frac{\varepsilon_{\gamma} - \varphi_{\gamma}}{\theta_{\gamma}}\right) - 1}, \quad f_{\pm} = \frac{1}{\exp\left(\frac{\varepsilon_{\pm} - \varphi_{\pm}}{\theta_{\pm}}\right) + 1},$$

where $\theta = kT/(mc^2)$ and $\varphi = \mu/(mc^2)$. Suppose $e^{\pm}\gamma \leftrightarrow e^{\pm'}\gamma'$ is in detailed balance. This means reaction rate vanishes

$$f_{\pm}(1 - f'_{\pm})f_{\gamma}(1 + f'_{\gamma}) = f'_{\pm}(1 - f_{\pm})f'_{\gamma}(1 + f_{\gamma}),$$

which leads to $\theta_{\gamma} = \theta_{\pm} \equiv \theta_k$. Analogous results for $e^{\pm}e^{\mp} \leftrightarrow \gamma_1\gamma_2$ leads to $\varphi_{\gamma} = \varphi_{\pm} \equiv \varphi_k$.

Only triple reactions give $\varphi_k = 0$!

Conservation laws

Energy conservation

$$\frac{d}{dt} \sum_i \rho_i = 0, \quad \text{or} \quad \frac{d}{dt} \sum_{i,\omega} Y_{i,\omega} = 0, \quad \text{where} \quad Y_{i,\omega} = \int_{\epsilon_{i,\omega} - \Delta\epsilon_{i,\omega}/2}^{\epsilon_{i,\omega} + \Delta\epsilon_{i,\omega}/2} E_i d\epsilon.$$

Particle's conservation for binary reactions

$$\frac{d}{dt} \sum_i n_i = 0, \quad \text{or} \quad \frac{d}{dt} \sum_{i,\omega} \frac{Y_{i,\omega}}{\epsilon_{i,\omega}} = 0.$$

Baryonic number and charge conservation respectively

$$\frac{dn_p}{dt} = 0, \quad n_- = n_+ + n_p,$$

The condition for the chemical potentials

$$\varphi_+ + \varphi_- = 2\varphi_\gamma.$$

Kinetic equilibrium 1

For photons we have

$$n_\gamma = \frac{1}{V_0} \exp\left(\frac{\nu_\gamma}{\theta}\right) 2\theta^3, \quad \frac{\rho_\gamma}{n_\gamma mc^2} = 3\theta, \quad V_0 = \frac{1}{8\pi} \left(\frac{2\pi\hbar}{mc}\right)^3$$

for pairs

$$n_\pm = \frac{1}{V_0} \exp\left(\frac{\nu_\pm}{\theta}\right) j_1(\theta), \quad \frac{\rho_\pm}{n_\pm mc^2} = j_2(\theta),$$

and for protons

$$n_p = \frac{1}{V_0} \sqrt{\frac{\pi}{2}} \left(\frac{M}{m}\right)^{3/2} \exp\left(\frac{\nu_p - M/m}{\theta}\right) \theta^{3/2}, \quad \frac{\rho_p}{M n_p c^2} = 1 + \frac{3}{2} \frac{m}{M} \theta,$$

$$j_1(\theta) = \theta K_2(\theta^{-1}) \rightarrow \begin{cases} \sqrt{\frac{\pi}{2}} e^{-\frac{1}{\theta}} \theta^{3/2}, & \theta \rightarrow 0 \\ 2\theta^3, & \theta \rightarrow \infty \end{cases},$$

$$j_2(\theta) = \frac{3K_3(\theta^{-1}) + K_1(\theta^{-1})}{4K_2(\theta^{-1})} \rightarrow \begin{cases} 1 + \frac{3}{2}\theta, & \theta \rightarrow 0 \\ 3\theta, & \theta \rightarrow \infty \end{cases}.$$

Kinetic equilibrium 2

Summing up energy densities

$$\sum_i \rho_i = \frac{mc^2}{V_0} \left\{ 6\theta^4 \exp\left(\frac{\nu_+}{\theta}\right) \left[1 - \frac{n_p V_0}{j_1(\theta)} \exp\left(-\frac{\nu_+}{\theta}\right) \right]^{\frac{1}{2}} + \right. \\ \left. + j_2(\theta) \left[2j_1(\theta) \exp\left(\frac{\nu_+}{\theta}\right) - n_p V_0 \right] + \frac{M}{m} \left(1 + \frac{3}{2} \frac{m}{M} \theta \right) n_p V_0 \right\},$$

and analogously for number densities

$$\sum_i n_i = \frac{1}{V_0} \left\{ 6\theta^4 \exp\left(\frac{\nu_+}{\theta}\right) \left[1 - \frac{n_p V_0}{j_1(\theta)} \exp\left(-\frac{\nu_+}{\theta}\right) \right]^{\frac{1}{2}} + 2j_1(\theta) \exp\left(\frac{\nu_+}{\theta}\right) \right\},$$

so that two unknowns, ν_+ and θ can be found.

Kinetic equilibrium 3

$$\exp\left(\frac{\nu_-}{\theta}\right) = \exp\left(\frac{\nu_+}{\theta}\right) + \frac{n_p V_0}{j_1(\theta)},$$

$$\exp\left(\frac{\nu_\gamma}{\theta}\right) = \exp\left(\frac{\nu_+}{\theta}\right) \left[1 + \frac{n_p V_0}{j_1(\theta)} \exp\left(-\frac{\nu_+}{\theta}\right)\right]^{\frac{1}{2}},$$

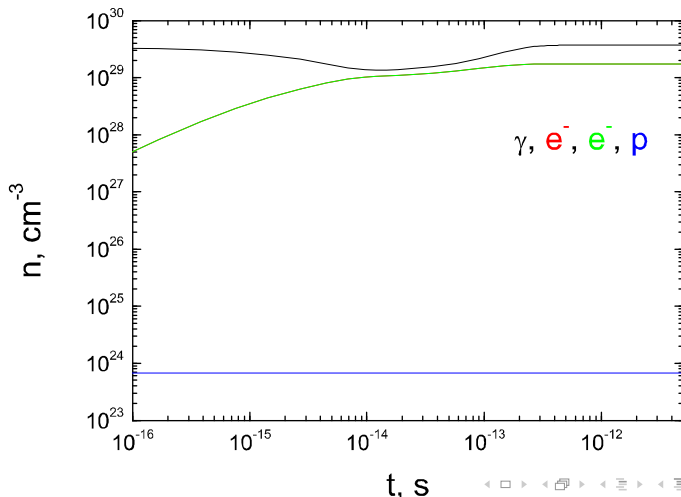
$$\exp\left(\frac{\nu_p - M/m}{\theta}\right) = n_p V_0 \sqrt{\frac{2}{\pi}} \left(\frac{m}{M}\right)^{3/2} \theta^{-3/2}.$$

In thermal equilibrium $\nu_\gamma = 0$ and $\nu_+ = -\nu_-$.

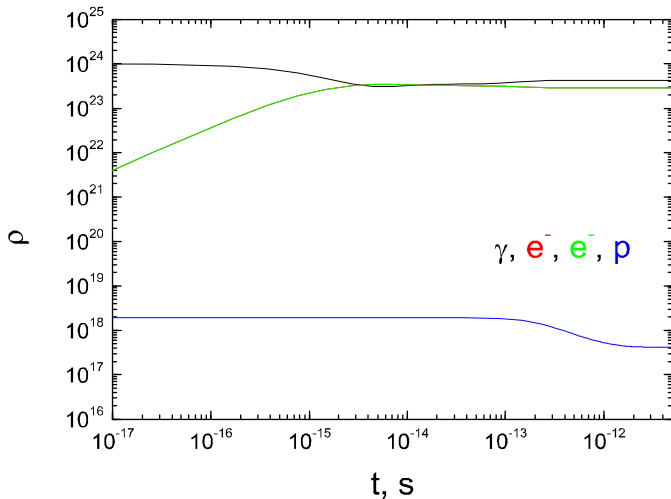
For $n_p > 0$ one always has $\nu_- > 0$ and $\nu_+ < 0$ in thermal equilibrium.

Concentrations

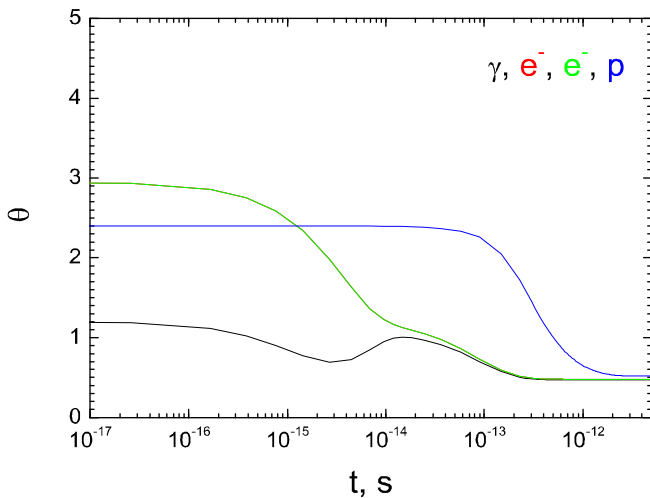
Initial conditions: $\rho = 10^{24} \text{ erg/cm}^3$, $\rho_{\pm} = 10^{-5}\rho$, $B = 10^{-3}$



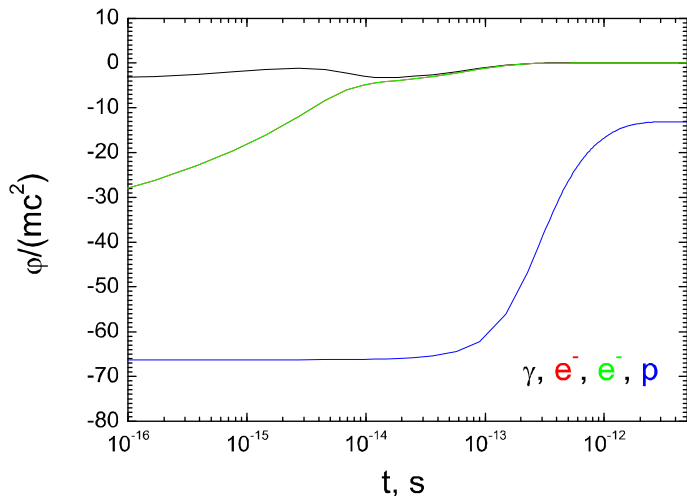
Energy densities



Temperatures



Chemical potentials



Conclusions

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- ② Kinetic equilibrium is obtained from the first principles.
- ③ Protons thermalize with other particles by proton-electron scatterings; proton-proton scattering is inefficient.
- ④ **The timescale of thermalization is always shorter than the dynamical one.**